

## Determination of acid dissociation constants based on continuous titration by feedback-based flow ratiometry

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### Abstract

We propose a method for the determination of acid dissociation constants based on the rapid detection of the equivalence point (EP) by feedback-based flow ratiometry and the subsequent estimation of the half equivalence point ( $EP_{1/2}$ ). The titrant (e.g., NaOH) flow rate  $F_B$  was varied in response to a control voltage  $V_c$  from a controller, while the titrand (e.g.,  $CH_3COOH$ ) flow rate  $F_A$  was held constant. The pH of the mixed solution was monitored downstream from the confluence point of the solutions following a knotted tubular mixer. Initially,  $V_c$  was increased linearly. At the instance the detector sensed EP, the ramp direction of  $V_c$  changed downward. The pH increased further because of the lag time between the mixing of solutions and the sensing of pH. Following the pH maximum, the pH decreased. The EP was sensed again in this downward scan. The  $V_c$  that gives  $EP_{1/2}$  was computed from the  $V_c$  just at the time of the EP detection. The  $V_c$  was held constant at this level for 18 s, and the plateau pH value thus obtained was taken to be the  $pK_a$  of the analyte subject to activity corrections. Studies on the dependence of the  $pK_a$  on the ionic strength or dielectric constant of the solution were conducted in an automated fashion by delivering NaCl solution or acetonitrile through an additional channel. Satisfactory results were obtained with good throughput (53 s per determination) and precision (R.S.D.  $\approx 0.3\%$ ) for various acids.

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**Keywords:** Flow ratiometry; Flow titration; Feedback-based control; Dissociation constant; Acidity constant

### 1. Introduction

Flow ratiometry, originated with Blaedel and Laessig [1,2], is a special class of continuous flow analysis, where two independently delivered solutions (e.g., titrand and titrant) are merged at various flow ratios  $R_f$ . Analytical signal  $V_d$  is monitored at a position downstream of the confluence point of the solutions. The information of interest is determined by analyzing the relationship between  $R_f$  and  $V_d$ . We have applied the method to continuous on-line titrations [3–5]. The scan range of  $R_f$  was limited to a domain just around the equivalence point (EP) by feedback-based control, to realize extremely high throughput titrations (e.g., 3 s per titration [3]). In other related work on the determination of distribution coefficients  $K_D$  of an analyte between two phases [6,7], the flow ratio of organic/aqueous flow

streams was changed stepwise in order to produce steady analytical signals corresponding to each flow ratio. The throughput of such measurements has recently been improved to 5 min per determination by detecting both phases on-line without phase separation [8].

The acid dissociation constant  $K_a$  is just as important as  $K_D$  for predicting and explaining the physicochemical and/or biological functions. Generally, an unionized molecule is more lipid soluble and thus penetrates more readily through biological membranes. In such a system, microscopic conditions around the molecules may easily vary and affect the  $K_a$ . Fast methods of  $K_a$  determination in which the matrix can be readily varied are therefore particularly important to understand the behavior of molecules in complex biological/environmental matrices. Several studies utilizing the paradigms of flow injection analysis (FIA) [9–13] and related techniques [14,15] have been carried out for this purpose; this was discussed elsewhere [16]. More recently, Box et al. [17] reported the  $K_a$  for 71 drugs based on a continuous flow scheme with a photodiode array detector. In their

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study, the sample flow was merged with a buffer of temporally changing pH created by mixing “linear buffer” solutions [18] respectively with added HCl and KOH, at different ratios as a function of time. A linear buffer based system for creating a pH gradient using a FIA system was introduced much earlier [9].

In our previous paper [16], feedback-based flow ratiometry was used for the rapid determination of  $K_a$ . In this approach, titrant (NaOH) flow rate was varied with the total (titrant + titrand) flow rate maintained constant. The half equivalence point ( $EP_{1/2}$ ) was directly determined by rapid upward and downward scans of titrant/titrand flow ratio. The method was applied to low molecular *n*-alkyl carboxylic acids ( $C = 1-5$ ) and  $H_3PO_4$ . High throughput (ca. 26 s per determination) was attainable with reasonable precision (relative standard deviation (R.S.D.)  $\approx 3\%$ ). The method was, however, susceptible to detector noise, although the bias in  $pK_a$  caused by the noise did not seem to be significant. Nevertheless, extensive noise filtration is required to improve reliability and this is incompatible with high throughput [19]. The determination of EP is less affected by noise [3–5] because the pH jump around EP is large compared to the noise. In the present study, we therefore explored an alternative approach for  $K_a$  determination through the detection of EP by feedback-based flow ratiometry and the succeeding estimation of  $EP_{1/2}$ . Compared to the previous approach [16], the presently proposed method needs a little longer time (53 s per determination), but the precision is improved by an order of magnitude (R.S.D.  $\approx 0.3\%$ ).

## 2. Experimental

### 2.1. Flow system

Fig. 1 shows the flow system. Two peristaltic pumps ( $P_1$  and  $P_2$ ; Rainin Dynamax RP-1) were used for delivering titrand (A) and titrant (B), respectively. Both solutions were continuously helium-degassed in order to prevent the influence of  $CO_2$  from ambient air. The experimental environment was air-conditioned at  $25^\circ C$ , but beyond this the experimental temperature was not controlled. The pump tubes used were 0.51 mm i.d. Pharmed<sup>®</sup> tubing. The flow rate  $F_A$  of a titrand was held constant at  $0.50\text{ cm}^3\text{ min}^{-1}$ . The flow rate  $F_B$  of a titrant ( $0.1\text{ mol dm}^{-3}$  NaOH or HCl) varied in response to a control voltage  $V_c$  (0–5 V) generated from an algorithm-based controller (PC; Toshiba Dynabook Satellite 1800 SA95C/4 notebook computer) through a PC card (Measurement Computing PC-CARD-DAS16/12-AO). Code written in Visual BASIC<sup>®</sup> in-house was used to generate  $V_c$ , acquire data, analyze them and graphically display the results. The titrant and titrand were merged in a polypropylene-tee and led to a mixing reactor (MR; 0.5 mm i.d., 50 cm long PTFE (Teflon) knotted tubing). The mixed solution was allowed to come into a flow cell (FC; Horiba 6941-15C flow-through glass electrode) equipped

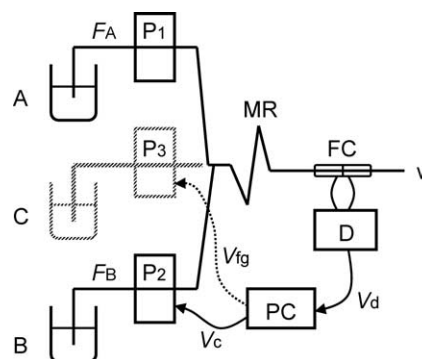


Fig. 1. Flow diagram of a flow ratiometry system. (A) Titrand (typically  $0.1\text{ mol dm}^{-3}$  acid); (B) titrant (typically  $0.1\text{ mol dm}^{-3}$  NaOH); (C) additive ( $2\text{ mol dm}^{-3}$  NaCl or acetonitrile); W, waste;  $P_1$ – $P_3$ , peristaltic pump; MR, mixing reactor; FC, flow cell (flow-through glass electrode equipped with a reference electrode); (D) pH meter; PC, controller (notebook computer).  $F_A$  and  $F_B$  are the flow rates of titrant and titrate, respectively.  $V_c$  and  $V_{fg}$  are the controller output voltages for titrant and additive flow rates, respectively.  $V_d$  is the detector output. For the  $pK_a$  determination in the presence of NaCl or acetonitrile, the third channel shown by the broken lines was added to the system.

with a reference electrode (Horiba 2461A-15T), both the electrodes being connected to a Horiba F-13 pH meter (D). The electrode was calibrated daily before the measurements with commercial standard pH buffers in flow mode. Output signal ( $V_d$ ) from the pH meter ( $-0.7$  to  $+0.7\text{ V}$  for pH 0–14) was digitized by the PC card at the frequency of 10 Hz and the resulting data were directly acquired in the Microsoft Excel<sup>®</sup> format.

In some experiments, the third channel shown by the broken lines in Fig. 1 was used for automatically changing the ionic strength or the dielectric constant (permittivity). Sodium chloride ( $2\text{ mol dm}^{-3}$ ) or acetonitrile was delivered by using the third pump ( $P_3$ ; the same model as  $P_1$  and  $P_2$ ). The pump speed of  $P_3$  could also be varied automatically by using another controller output voltage ( $V_{fg}$ ) from the controller.

### 2.2. Reagents

Reagents (analytical reagent grade; Kanto Chemicals or Nacalai Tesque) were used without further purification. Milli-Q SP grade deionized water was used throughout.

## 3. Principles

Fig. 2 illustrates the principle of the present method by using real data for the titration of  $0.1\text{ mol dm}^{-3}$   $CH_3COOH$  with  $0.1\text{ mol dm}^{-3}$  NaOH. Initially, the controller output voltage  $V_c$ , and thus the NaOH flow rate  $F_B$  increases linearly. The value of  $V_c$  determines the composition of the mixed solution at the confluence point of both the solutions. The pH of the mixed solution being detected increases after a delay. This delay is primarily determined by the physi-



## 4. Results and discussion

### 4.1. System set-up

The scan rate of  $V_c$  was investigated in the range of  $5\text{--}100\text{ mV s}^{-1}$  by using  $0.1\text{ mol dm}^{-3}$   $\text{CH}_3\text{COOH}$  and  $0.1\text{ mol dm}^{-3}$   $\text{NaOH}$  as titrand and titrant, respectively. The  $\text{pK}_a$  values obtained are plotted as a function of the scan rate in Fig. 3 along with  $\pm 1$  standard deviation depicted as the error bar. While the effect of scan rate on the mean  $\text{pK}_a$  value obtained was insignificant, it obviously had large effect on the precision of the measurement. The rate of pH change increases as the scan rate (and hence the titrand flow rate) increases. Operationally, this made it more difficult to locate EP precisely at high scan rates, resulting in large uncertainties at scan rates  $>60\text{ mV s}^{-1}$ . Scans rates  $\geq 90\text{ mV s}^{-1}$  sometimes failed to find EP altogether because, depending on the  $\text{pK}_a$ , the titrand concentration and the presence of the finite transit time,  $V_c$  may reach its scan limit (0 or 5 V) before EP is detected. On the other hand, scan rates of  $\leq 10\text{ mV s}^{-1}$  also failed to find EP because the slope of the titration curve decreased sufficiently to render the detection of EP more susceptible to detector noise. The effect of the scan rate was further investigated at 30, 40 and  $50\text{ mV s}^{-1}$  by applying the method to several  $n$ -alkyl carboxylic acids ( $C = 1, 3\text{--}5$ ) and  $\text{H}_3\text{PO}_4$ . The best results were obtained at the scan rate of  $40\text{ mV s}^{-1}$  and further work was conducted at this scan rate.

The effects of the nature and the length of the mixing reactor were examined by using knotted tubular reactors (0.5 mm i.d.; 25, 50 or 100 cm long, knot diameter  $\sim 0.5$  cm) [21] and single bead string reactors (1 mm i.d.; 5, 10 or 20 cm long; 0.6 mm bead diameter). The relative standard deviation (R.S.D.) of  $\text{pK}_a$  for  $\text{CH}_3\text{COOH}$  was  $\leq 0.3$  and  $\leq 0.6\%$  for the two reactor types, respectively, with no significant effect of the reactor length within the range examined. Further work was therefore conducted with a 50 cm knotted tubular reactor.

Data acquisition frequency and noise filtration techniques were investigated to see if the reliability of the measurement can be improved by varying those parameters. From the results for extensive sets of the experimental tests, we selected

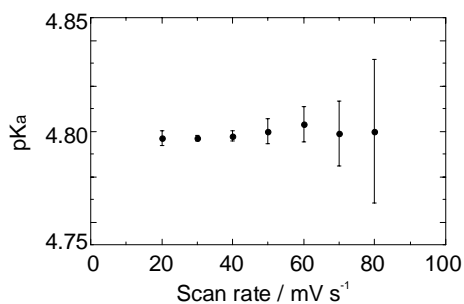


Fig. 3. Effect of scan rate on the  $\text{pK}_a$  and its standard deviation of  $\text{CH}_3\text{COOH}$ . Titrand and titrant are the same as those in Fig. 2.

$10\text{ Hz}$  as data acquisition frequency. A moving average filter that used 11 consecutive raw  $V_d$  values was utilized and the data thus generated was processed a second time through an identical filter.

In contrast to the previous approach [16], where  $\text{EP}_{1/2}$  is determined directly, the present approach requires the calibration of flow rates because  $V_{eq}$  and thus  $V_{1/2}$  are expressed as a function of both  $F_A$  and  $F_B$  (see Eq. (10)). If the flow rate changed from the calibrated values, this error can affect the estimation of  $V_{1/2}$ . In order to ascertain the extent of this influence, we intentionally biased  $F_A$  or  $k (=F_B/V_c)$  to slightly erroneous values as software parameters and compared the  $\text{pK}_a$  of  $\text{CH}_3\text{COOH}$  thus obtained with that determined with the correct values of  $F_A$  and  $k$ . Errors in  $F_A$  ranging from  $-10, -5, -1, +1, +5$  to  $+10\%$  were found to cause  $-0.004 \pm 0.004, -0.001 \pm 0.007, +0.0003 \pm 0.007, +0.0005 \pm 0.014, -0.006 \pm 0.006\%$  and  $-0.018 \pm 0.004$  errors in  $\text{pK}_a$ , respectively. Similar variations in  $k$  caused  $+0.006 \pm 0.020, -0.005 \pm 0.015, +0.005 \pm 0.007, +0.001 \pm 0.005, +0.009 \pm 0.016$  and  $+0.052 \pm 0.006$  errors, respectively ( $n = 3\text{--}5$ ). The maximum bias in  $\text{pK}_a$  was  $-0.018$  (relative error 0.39%) resulting from a  $+10\%$  error in  $F_A$ . The fact that the buffer capacity of the mixed solution is maximum at  $\text{EP}_{1/2}$  makes the determined value of  $\text{pK}_a$  relatively insensitive to the various possible sources of error.

### 4.2. Applications to various acids and bases

The dissociation constants of various acids and bases as determined by the present method are listed in Table 1 along with the literature values [22–25]. In the case of  $\text{H}_2\text{CO}_3$  and  $\text{NH}_4^+$ , their conjugate bases ( $\text{CO}_3^{2-}$  (taken as  $\text{Na}_2\text{CO}_3$ ) and  $\text{NH}_3$ ) were titrated with  $0.1\text{ mol dm}^{-3}$   $\text{HCl}$ . For  $\text{H}_3\text{PO}_4$  and  $\text{H}_2\text{CO}_3$ , the first or second dissociation constants were independently determined by presetting the lower and upper pH limits for the EP detection so as to confine the system to the desired titration step. For example, pH 3–6 and 8–12 were the respective set limits for the first and the second titration steps of  $\text{H}_3\text{PO}_4$ . The values obtained by the present automated approach were in good agreement with the literature data. the largest standard deviations was maximally 0.076 for the  $\text{pK}_{a2}$  of  $\text{H}_3\text{PO}_4$ , amounting to 1.05% in R.S.D.

### 4.3. Effect of ionic strength or dielectric constant

By using the configurations with three pumps (Fig. 1),  $\text{NaCl}$  or acetonitrile ( $\text{MeCN}$ ) was delivered at various flow rates. The results for the titration of  $\text{CH}_3\text{COOH}$  with  $\text{NaOH}$  in the presence of  $\text{NaCl}$  and  $\text{MeCN}$  are plotted together in Fig. 4. The  $V_{fg}$  (the control voltage for  $P_3$  pump) was increased and then decreased stepwise during the period of 50 min. In this period, the concentrations of  $\text{NaCl}$  and  $\text{MeCN}$  at  $\text{EP}_{1/2}$  level were changed between 0 and  $1.14\text{ mol dm}^{-3}$  and between 0 and 40 vol.%, respectively. For pH measurement over a long period, the software was modified to prevent data overflow ( $>65,536$  lines). In this version, the most



Table 1  
Dissociation constants of acids determined by flow ratiometry

Analyte		$pK_a$	S.D. ( $n$ )	Literature values <sup>a</sup>
Formic acid (HCOOH)		3.761	0.007 (4)	3.75 [22,23]
Acetic acid (CH <sub>3</sub> COOH)		4.784	0.002 (3)	4.756 [22], 4.76 [23]
Propanoic acid (C <sub>2</sub> H <sub>5</sub> COOH)		4.877	0.001 (4)	4.87 [22,24], 4.88 [23]
<i>n</i> -Butanoic acid (C <sub>3</sub> H <sub>7</sub> COOH)		4.855	0.007 (8)	4.82 [23], 4.83 [22]
<i>n</i> -Pentanoic acid (C <sub>4</sub> H <sub>9</sub> COOH)		4.873	0.010 (8)	4.83 a [22]
Phosphoric acid (H <sub>3</sub> PO <sub>4</sub> )	$pK_{a1}$	2.095	0.012 (4)	2.15 [25], 2.16 [22]
	$pK_{a2}$	7.206	0.008 (4)	7.20 [25], 7.21 [22]
Ammonium ion (NH <sub>4</sub> <sup>+</sup> )		9.287	0.003 (6)	9.25 [22]
Carbonic acid (H <sub>2</sub> CO <sub>3</sub> )	$pK_{a1}$	6.313	0.021 (9)	6.35 [22]
	$pK_{a2}$	10.611	0.019 (9)	10.33 [22]

<sup>a</sup> At 25 °C except for the value denoted by the letter “a” (20 °C).

recent 1000 data points for  $V_c$ , pH and  $dpH/dt$  were collected and displayed as in Fig. 2, whereas  $V_{fg}$  (5 s resolution) and the value of  $pH_{1/2}$  at  $EP_{1/2}$  are collected and displayed over the whole measurement period (Fig. 4). Similar experiments were carried out for the titration of NH<sub>3</sub> with HCl in the ranges of NaCl and MeCN concentrations 0–0.57 mol dm<sup>−3</sup> and 0–40 vol.%, respectively.

The  $pK_a$  values of CH<sub>3</sub>COOH and NH<sub>4</sub><sup>+</sup> measured as a function of ionic strength (that contributed by CH<sub>3</sub>COO<sup>−</sup>, H<sup>+</sup>, NH<sub>4</sub><sup>+</sup> and OH<sup>−</sup> at  $EP_{1/2}$  was also included) in the presence of NaCl are shown as the closed circles and triangles, respectively, in Fig. 5A. The two open symbols are the respective literature values [22]. The results seem reasonable because the determined values of  $pK_a$  with activity correction are almost constant irrespective of the ionic strength.

For the measurement of pH in a mixed solvent, the electrode should be calibrated with standard pH buffers in the same solvent as samples. Such a procedure can be implemented in the present system but at the expense of considerable complexity. Presently, the pH in mixed solvent ( $s_w$ pH) was measured by using an electrode pre-calibrated with aqueous standard buffers. Then, this  $s_w$ pH was corrected by taking into account the mole fraction of MeCN,  $X_{MeCN}$ , by the experimentally obtained equation following the rec-

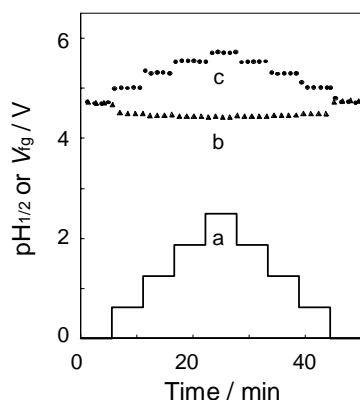


Fig. 4. The  $pK_a$  determination of CH<sub>3</sub>COOH in matrices of changing composition. (a)  $V_{fg}$ ; (b and c) pH at the half equivalence point in the presence of NaCl and acetonitrile, respectively.

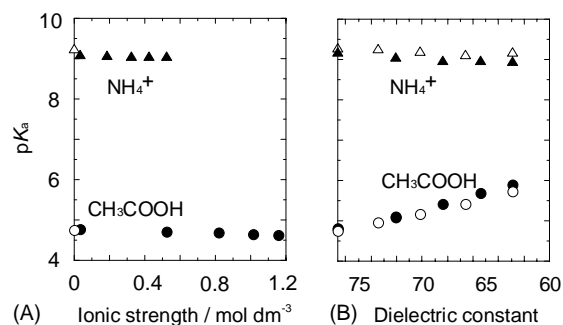


Fig. 5. Effect of ionic strength (A) and dielectric constant (B) on the  $pK_a$  of CH<sub>3</sub>COOH and NH<sub>4</sub><sup>+</sup>. Closed and open symbols are the experimental and literature values of  $pK_a$ .

ommendations in [26]:

$$s_{sp}pH = s_w pH + 3.81 X_{MeCN} \quad (12)$$

where  $s_{sp}$ pH means the pH in a MeCN–H<sub>2</sub>O medium, referred to the standard pH buffers containing MeCN at the same  $X_{MeCN}$  as in the sample. Thus corrected  $s_{sp}pK_a$  is shown in Fig. 5 by the closed symbols as a function of the dielectric constant. The dielectric constant ( $\epsilon$ ) of the MeCN–H<sub>2</sub>O media were estimated from the Eq. (13) [26].

$$\epsilon^{-1} = 0.01547 X_{MeCN} + 0.01305 \quad (13)$$

The values obtained in the present experiments (Fig. 5B) agreed well with the literature values [26,27] (shown as open symbols); the  $pK_a$  values for CH<sub>3</sub>COOH (closed circles) increased with decreasing  $\epsilon$  and those for NH<sub>4</sub><sup>+</sup> (closed triangles) were almost constant irrespective of  $\epsilon$ . From these results, we concluded that the present system is capable of accurately determining  $pK_a$  in matrices of high ionic strength and lower dielectric constant, at least within the realm of the experiments presently conducted.

## 5. Conclusion

We have applied feedback-based flow ratiometry for the determination of acidity constants based on the rapid de-

termination of the equivalence point (EP) and the subsequent measurement of the half equivalence point ( $EP_{1/2}$ ). The present method can determine a  $pK_a$  value with high precision ( $\leq 0.3\%$  R.S.D.) in under 1 min, thus making it useful for rapid estimation of  $K_a$  for a variety of compounds in varying matrices.

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